# Why Is There a Glass Ceiling for Threading Based Protein Structure Prediction Methods?

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**ABSTRACT:** Despite their different implementations, comparison of the best threading approaches to the prediction of evolutionary distant protein structures reveals that they tend to succeed or fail on the same protein targets. This is true despite the fact that the structural template library has good templates for all cases. Thus, a key question is why are certain protein structures threadable while others are not. Comparison with threading results on a set of artificial sequences selected for stability further argues that the failure of threading is due to the nature of the protein structures themselves. Using a new contact map based alignment algorithm, we demonstrate that certain folds are highly degenerate in that they can have very similar coarse grained fractions of native contacts aligned and yet differ significantly from the native structure. For threadable proteins, this is not the case. Thus, contemporary threading approaches appear to have reached a plateau, and new approaches to structure prediction are required.
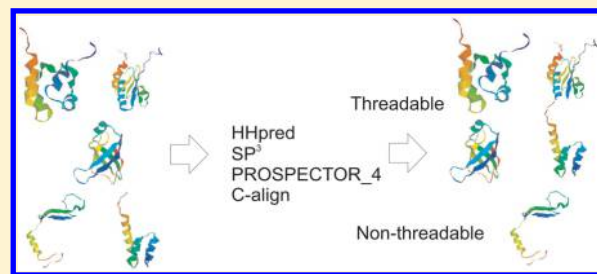
## INTRODUCTION

One of the more perplexing observations that comes out of the CASP protein structure prediction experiments is that, despite the diversity of implementations[1-7] (different profiles,[8-10] dynamic programming,[11] hidden Markov models,[12,13] use or absence of predicted contacts,[14,15] and/or pair potentials[16-20]), for target proteins lacking closely homologous templates in the Protein Data Bank (PDB),[21] the best threading based methods tend to recognize the same targets as being threadable or nonthreadadble.[2] Put another way, with few exceptions associated with the actual alignment quality and the rare case where one class of threading algorithms does better than the others, the performance of different threading algorithms is remarkably similar. This pattern goes back to very early CASPs and persists to the present.[2,22] Key questions are why is this the case and does it suggest that for proteins lacking close homologues the performance of classical threading approaches has reached a plateau, much as secondary structure predictions schemes did over a decade ago?[23-28] If it indeed turns out that there are certain classes of protein structures that preclude them from having successful predictions in the absence of closely homologous templates, then this would suggest that, for these proteins, alternative nonthreading based methods of protein structure prediction are required. If so, the further development of classical threading based approaches would likely experience limited success.

In practice, this issue is important, because threading based structure prediction methods have the most general applicability for predicting protein structure,[29,30] with ~86% of human proteins having at least one domain predicted with acceptable accuracy (with TM-scores $\geq 0.4$[19,31,32] to native, with a TM-score of 1.0 indicating identical structures and tertiary structures with TM-scores above the 0.4 threshold

having p-values at or below $10^{-5}$) for virtual ligand screening,[32-35] for functional analysis,[36] as well as to assist in the identification of disease associated missense variations.[37] Complementary to threading based approaches are template free methods;[38,39] among the most successful are those that use residue covariation to predict tertiary contacts.[40-44] However, to accurately predict contacts from correlated mutation analysis requires that there be a very large number of protein sequences in a given family. At present, this limits the general applicability of this promising and yet quite old methodology. Thus, as a practical matter, at present threading based approaches afford the largest coverage of proteins. As such, it is important to understand why they fail, as this might motivate the development of more powerful threading based methods.

The most important factor that influences the performance of a given threading algorithm is the comprehensiveness of the protein structure template library. The performance of a given threading algorithm can drastically change depending on whether or not closely homologous templates are included in the template library. While in principle the same set of PDB structures are available to all investigators at the time of a given CASP, in practice, the template libraries used by different laboratories are often somewhat different. In general, this cannot be a major effect, since essentially all of the best threading algorithms perform similarly.[1,2,4,5] However, to be absolutely certain that different state of the art threading algorithms perform similarly requires that the template library

used by the different algorithms be exactly the same. In that regard, for those cases where threading fails, it is possible that the template library lacks sufficiently close structures that its failure is simply due to the absence of suitable structural templates. This would imply that the PDB library is not complete, a result in contradiction with a significant body of work,[45,46] but one which has to be investigated. As a corollary, there might be suitable templates in the PDB, but the substructure that aligns to the target contains so many gaps that threading based methods cannot work—the cost of introducing many gaps in the threading alignment is too high. Another possible explanation is that certain proteins are so evolutionarily distant from their templates that threading based methods, which are inherently driven by profile similarity, fail. If so, it should be reflected in the set of sequences used to construct the sequence profiles rather than the structure itself. This issue can be directly addressed by computationally generating sequences that in the context of a given potential have low energy in the structure of interest,[47,48] and examining if there are any common features between structures that are threadable when native and such artificial sequences are used. If in the majority of cases virtually the same sets of structures are threadable or nonthreadable, this would imply that there is (are) some features of the structure responsible for its threadability. In this context, we could use a purely structure based algorithm to detect which structural features of the fold are responsible for the success or failure of threading. In the simplest case, one could just align secondary structural elements; however, different folds can have closely matching, if not absolutely identical, secondary structures. On the other hand, $C\alpha$-based contacts could potentially differentiate between protein structures. This might be true when a significant fraction of the contacts in the structure are nonlocal; whereas if most contacts are local, one is really comparing local secondary structures rather than global folds. One also has to bear in mind that, for distantly related pairs of proteins, even if one had native contacts in hand, due to differences in the structures, 100% of their contacts need not overlap. In that regard, when the number of secondary structures is small, viz., the folds are of low complexity, one might also expect significant contact overlap, yet their global folds might differ appreciably.

The goal of this paper is to understand why certain classes of proteins are nonthreadable while others are threadable. We examine each of the possible underlying causes described above and explore whether the nonthreadability of distantly homologous proteins is predominantly a feature of the target protein's structure or is due to differences in the evolutionary distance of the target from the closest template structures. By focusing on the structural properties of these proteins, we demonstrate that the difficulty in threading experiences is due to the inherent features of threadable vs nonthreadable protein structures. Finally, we discuss promising existing and to be developed approaches that can extend protein structure prediction to enable it to consistently break through the glass ceiling of threading based protein structure prediction methods.

## ■ METHODS

**Template and Target Libraries, Threading Algorithms, and Assessment Metrics.** A representative PDB template library that is an extension of the PROSPECTOR_4 template library[49] clustered at the level of 35% sequence identity was prepared. This library, LIST.templates, consists of 16,747 proteins ranging in length from 40 to 1962 residues.

The representative set of target proteins, LIST.targets, consists of 3221 proteins that share no more than 35% pairwise sequence identity and range in length from 40 to 200 residues. Both libraries as well as the list of threadable and nonthreadable proteins are available at http://cssb2.biology.gatech.edu/threading/download.html.

To assess whether the majority of templates are recognized by different threading algorithms, we employed HHpred,[50,51] SP3,[9] and PROSPECTOR_4;[49] for details of these algorithms, we refer the reader to the original papers. These three algorithms were chosen because they use different alignment methods and types of scoring functions. For each threading algorithm, the same threading library, LIST.templates, was employed as well as the sequence data set used to build the appropriate sequence profiles. This will allow for direct evaluation of the conjecture that there is (are) some property(ies) of the target structure that render them threadable or nonthreadable. In that regard, a metric of structure comparison between the target structure and threading alignment to the template protein is required. To assess a given threading alignment, we employ the TM-score[52] generated using the latest version fr-TM-align,[53] an improved, more sensitive version of the original TM-align protein structure alignment algorithm.[31] As previously, we define a protein as being threadable if its TM-score is ≥0.4.

**Generation of Low Energy Artificial Protein Sequences for the Target and Template Structures.** For each PDB target and template protein, following the procedure described in ref 47, low energy sequences for the given structure were generated. The potential consists of burial, secondary structure, and pair statistical potentials. For a given randomly selected overall amino acid composition whose average matches that in the PDB, the sequence is shuffled until a low energy sequence is found. Then, the process is repeated until 60 such low energy sequences are generated for each target and template protein structure. Note that the average pairwise sequence identity is about 11% for the set of low energy sequences that match the given structure. We then use the resulting sequences to generate the sequence profile for use in threading by PROSPECTOR_4.[49]

**C-Align: A $C\alpha$-Based Contact Map Alignment Algorithm.** In what follows, we describe C-align, a newly developed $C\alpha$-based contact map based alignment algorithm. It aligns a pair of structures based on the overlap of the set of contacts defined between residues $i$ and $j$ whose distances between pairs of $C\alpha$ atoms are less than $d = 8.5$ Å, $C(i, j)_{8.5}$, and $d = 14$ Å, $C(i, j)_{14}$, respectively. Here,

$$C_d(i, j) = \begin{cases} 1 & \text{if} \quad d_{ij} \leq d \\ 0 & \text{if} \quad d_{ij} > d \end{cases} \tag{1}$$

where $d_{ij}$ is the distance between $C\alpha$'s $i$ and $j$. We need to consider both short- and long-range contacts, i.e., contacts between residues that are <6 (short-range) and ≥6 (long-range) residues apart, respectively. In what follows, lower (upper) case residue indices, e.g., $i$ ($J$), refer to the $i^{\text{th}}$ ($J^{\text{th}}$) residue in the target (template) protein, respectively. Let $n^S(i)_d$ and $n^L(i)_d$ be the number of such short- and long-range contacts for residue $i$ in the target structure

$$n^\beta(i)_d = \sum_{l=1}^{n^\beta(i)} C_d(i, M_d(l, i)) \tag{2}$$

with $\beta$ = S or L and $M_d(l, i)$ the identity of the $l$th contacting residue with residue $i$.

Then, the first pass scoring function to generate the initial alignment given for a given $\gamma$ is given by

$$S^{1,L}(i, J) = (1/(1 + |n^L(i)_{8.5} - n^L(J)_{8.5}|^\gamma))$$
$$+ (1/(1 + |n^L(i)_{14} - n^L(J)_{14}|^\gamma)) \qquad (3)$$

Note that, as $\gamma$ increases, the scoring penalty for contact number mismatch grows as well. In practice, three independent runs will be done, where $\gamma = (2, 4, 6)$, respectively. Dynamic programming is implemented in an identical manner to that in PROSPECTOR_4.[49]

Following the first pass for a given $\gamma$, we then perform a series of 30 successive iterations. The score of a given alignment for the $K$th iteration is given as follows: Let $a\ln(J)^{K-1}$ be the alignment of template residue $J$ to target residue $i$ generated by the $(K - 1)$st alignment. Then, the number of correctly aligned contacts with a distance cutoff $d$ for residue $i = a\ln(J)$ is given by

$$o^\beta(i(J))_d^{K-1} = \delta_{i,a\ln^{K-1}(J)} \sum_{l=1}^{n^\beta(i)} C_d(i, M_d(l, i)) \sum_{T=1}^{N_T} \delta_{M_d(l,i),a\ln(T)}$$
$$(4)$$

where $\delta_{\varepsilon\zeta}$ is the Kronecker delta, $N_T$ is the number of template residues, and $T$ is the residue index. The score associated with aligning residue $i$ with residue $J$ is given by

$$S(i, J) = S^{K,L}(i, J) + 0.25 \times S^{K,S}(i, J) \qquad (5a)$$

where

$$S^{K,\beta}(i, J) = o^\beta(i(J))_{8.5}^{K-1} + o^\beta(i(J))_{14}^{K-1}$$
$$+ (1/(1 + |n^\beta(i)_{8.5} - o^\beta(i(J))_{8.5}|^\gamma))$$
$$+ (1/(1 + |n^\beta(i)_{14} - o^\beta(i(J))_{14}|^\gamma)) \qquad (5b)$$

The best of the successive set of alignments is chosen from the maximum value of the fraction of native contacts aligned in the template structure and is calculated for an $M$ residue target protein following the $K$th iteration by

$$f_N = \frac{\sum_{J=1}^{N_T} o_{14}^L(i(J))_{d_{14}}^K}{\sum_{i=1}^M n^L(i)_{14}} \qquad (6)$$

In practice, $f_N$ is obtained by iterating over a range of 11 gap opening and gap extension penalties, where the gap opening penalties range from $[-1, -2]$ and the gap extension penalties range from $[0, -0.9]$, and are decremented by $-0.1$ per iteration. In addition to generating the alignment over the entire template molecule, we consider alignments to template substructures. We first consider the template substructure from residues 6 to $N_T - 5$. The next substructure is from 11 to $N_T - 10$. The process is iterated up to a total of 10 times, each time successively decreasing the substructure's length by 10 residues, provided that the template is at least 10% longer than the target protein. The goal is to try and capture good substructure alignments to the template even when the global contact map overlap is quite poor. This was found to be necessary especially when the target and templates differ significantly in length. While in principle a perfect global search algorithm should find the best alignment, given that we employ an iterative dynamic programming algorithm, sometimes the alignment gets trapped

in deep local minima. This procedure helps alleviate this problem.

As a preliminary validation step, C-align was applied to generate the contact map alignment of the 3221 target proteins. 95.2% have a TM-score $\geq 0.95$, with 98% of the targets having greater than 95% of their native contacts recovered. We next compared the resulting best TM-score obtained from using C-align to that of the best structural alignment, SA, obtained from fr-TM-align on templates whose sequence identity to the target is $\leq 30\%$; for this comparison, the best SA templates are used in both cases. The correlation coefficient for their TM-scores is 0.93, with the full set of pairs of TM-scores shown in Figure 1.
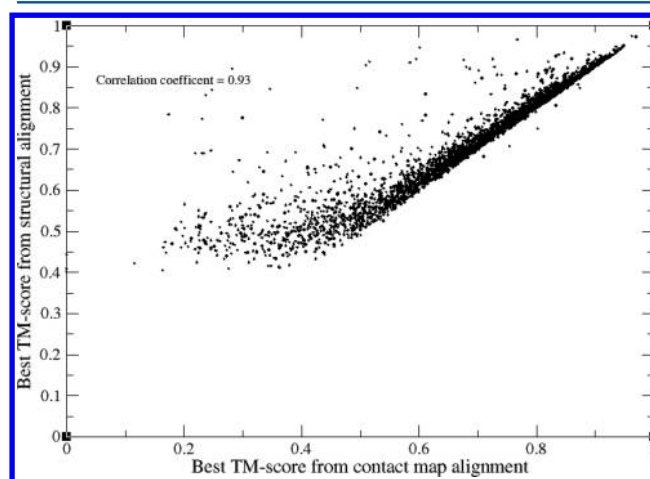


**Figure 1.** Comparison of the best TM-score obtained using C-align to the best structural alignment obtained from fr-TM-align on templates whose sequence identity to the target is $\leq 30\%$.

As expected, in almost all cases, the TM-score obtained from the best structural alignment $\geq$ the TM-score obtained from aligning contact maps, with the greatest discrepancy between the two methods found in the neighborhood of TM-scores of $<0.40$; see below for the discussion of these nonthreadable proteins. In this regime, the best contact map alignment need not produce the best TM-score, with the discrepancy generally decreasing as the TM-score increases. Nevertheless, these results show that C-align can generate good quality alignments. It will be used in what follows to help dissect what are the features of those proteins where threading fails.

Finally, in what follows, we will need to calculate the contact order of a given target from

$$co = \frac{\sum_{i=1}^M \sum_{j=1}^M C_{14}^L(i, j)|i - j|}{M} \qquad (7)$$

## RESULTS

**Do Different Threading Algorithms Perform Similarly on the Same Target Protein?** The first question that needs to be addressed is whether or not the failure of a given threading algorithm is due to the nature of the target structure or reflects differences among the various implementations of the different threading approaches. The latter is often the implicit expectation. However, as shown in Figure 2, this is not the case.

In the TM-score range $<0.5$, SP$^3$ performs the best, while HHpred generates better high quality alignments in the $>0.5$, high TM-score range. However, with regard to the ability to
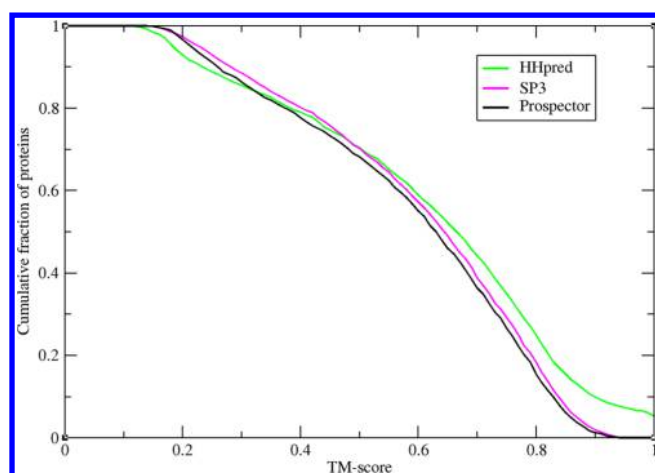
**Figure 2.** For the best of the top 5 ranked template alignments, the cumulative fraction of proteins whose TM-score ≥ TM-score on the *x*-axis.

identify suitable templates, the performance of all three approaches, despite the details of implementation, is remarkably similar. This conclusion is further reinforced in Figure 3
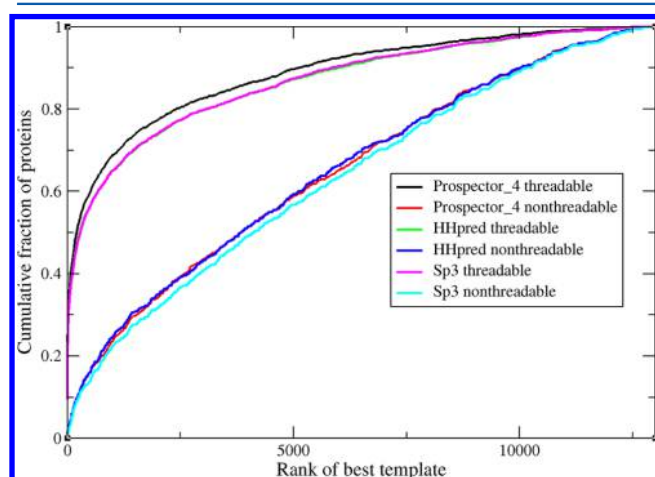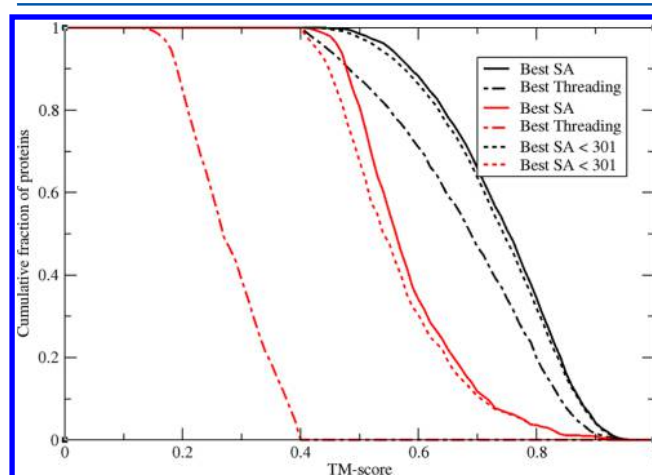


**Figure 3.** For both threadable and nonthreadable protein targets, the cumulative fraction of templates whose rank ≤ value indicated on the *x*-axis.

where for proteins that are threadable (the TM-score of the best of the top 5 ranked templates ≥ 0.4) and nonthreadable (TM-score < 0.4), we plot the rank of the very best template (whose threading TM-score is maximal) obtained by the three different threading approaches. In this case, the performances of HHpred and PROSPECTOR_4 are virtually identical, with SP$^3$ selected templates having slightly higher rank, with lower rank being better. Of course, it is possible that each of the three

algorithms on average performs better on mostly different protein targets, yet the average behavior is the same. That this is not the case at all is clearly demonstrated in Table 1.

Clearly, on the basis of Table 1, in no more than 6% of the cases are the same proteins classified as threadable by one algorithm and nonthreadable by the other. Indeed, 2323 proteins are assigned to be threadable by all three methods. Put another way, which proteins are threadable or not depends mainly on the target protein itself and not on the threading algorithm which is employed. In what follows, we wish to elucidate why this is the case.

**Are There Always Good Structures (TM-Score ≥ 0.4) in the Threading Template Library?** The most straightforward explanation for the fact that all three threading algorithms behave essentially the same is that for the nonthreadable targets there are no good structural templates in the template library, whereas for threadable proteins there are. That this is not the explanation is convincingly demonstrated in Figure 4, where we



**Figure 4.** For both threadable and nonthreadable protein targets, the cumulative fraction of templates whose best TM-score obtained by the structural alignment algorithm fr-TM-align, Best SA, and from PROSPECTOR_4, Best Threading. Threadable and nonthreadable targets are indicated in black and red, respectively.

plot the cumulative fraction of proteins whose best template TM-score obtained from the structural alignment algorithm fr-TM-align[53] versus best TM-score is presented. We also include the corresponding cumulative fraction for the best TM-score obtained from threading. While it is true that threadable templates have on average considerably higher TM-scores, in no case is there a target for which the best template structural alignment TM-score is not ≥0.4. To preclude the possibility that the best templates have a considerable number of gaps in the alignment (i.e., are discontinuous alignments in very large proteins with lots of gaps), we also plot the corresponding

**Table 1. Comparison of Threadable and Nonthreadable Targets in HHpred, SP$^3$, and PROSPECTOR_4**[a]

| algorithm | HHpred | | | | SP$^3$ | | | | PROSPECTOR_4 | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | TH-TH | TH-NTH | NTH-TH | NTH-NTH | TH-TH | TH-NTH | NTH-TH | NTH-NTH | TH-TH | TH-NTH | NTH-TH | NTH-NTH |
| HHpred | 2544 | 0 | 0 | 677 | 2471 | 73 | 113 | 563 | 2355 | 189 | 148 | 528 |
| SP$^3$ | 2471 | 113 | 73 | 563 | 2584 | 0 | 0 | 637 | 2392 | 192 | 111 | 526 |
| Prospector_4 | 2355 | 189 | 189 | 528 | 2392 | 111 | 192 | 526 | 2503 | 0 | 0 | 718 |

[a]X-Y, with X and Y = TH or NTH means that the given target is threadable, TH, or nonthreadable, NTH, in the first (X) and second (Y) members of the pair of compared threading algorithms.

distribution restricted to templates <301 residues. Again, the same behavior is clearly seen. What is also evident is that the difference in TM-scores of proteins from their best structural alignment is about 0.3 TM-score units for nonthreadable proteins and at most 0.1 TM-score units for threadable proteins. Thus, while nonthreadable targets have templates that are structurally more distant than their templates which are of poorer quality than threading targets, nevertheless there are certainly adequate templates in the PDB library to yield far better results than those obtained from threading. For the best templates, the very best templates have lower (higher) ranks when threadable (nonthreadable) proteins are used (see Figure 3) (lower ranks are better). Thus, more complex explanations of the cause of consensus nonthreadable targets are required.

**Comparison of Threading Results for Artificial and Native Protein Sequences.** For distantly related targets and templates, another possible origin of nonthreadable proteins is that they are evolutionarily more distant from their templates than threadable ones and/or they have too few sequences to construct sensitive sequence profiles. To examine this issue, we generated a set of 60 sequences with protein like, amino acid composition per target protein selected on the basis that they have a low, knowledge based force field[47] energy in the target structure. The average pairwise sequence identity of the sequences that adopt a given target fold is 11.9%, with a standard deviation of 1.1%. These targets were then threaded against a set of 12,532 templates (the subset of structures in LIST.templates <300 residues in length) whose sequence profiles are also generated from 60 artificial sequences/template. For each template protein structure, their mean pairwise sequence identity is 11.3%, with a standard deviation of 1.3%. PROSPECTOR_4 was then employed to thread these artificial targets to the artificial template structures. The mean sequence identity of the target/best threading template is 13.8%. 2141 have a TM-score to native in the best of the top 5 threading templates ≥0.4, viz., are threadable. Of these, 2027 are also threadable when native sequences are used. Similarly, for the nonthreadable targets, 603 are in common when artificial and native protein sequences are used.

Interestingly, as shown in Figure 5, the correlation coefficient between the TM-score of the best template obtained using native sequences to that using artificial sequences is 0.82. While there are clearly some differences as to which proteins are threadable and which are not, overall, the performance when artificial and wild type sequences are used is similar. Note that all artificial sequences when threaded to their native structure recover the native alignment; the issue is what happens when distantly related template structures are used. This observation was previously used in an attempt to help improve threading by using artificial template protein sequences in one incarnation of threading,[54] but as seen from the figure, the improvement is uneven.

Figure 5 also clearly shows that in reality threading need not in fact detect evolutionarily related sequences, as the majority of artificial sequences generated by the criterion of protein stability are also threadable. However, the two sets of sequences behave in a similar fashion as to which protein structures are threadable and which are not. The potentials used to generate the artificial sequences could provide a clue as to what in reality is driving selection/threadability. We first consider the case of threading by matching secondary structure alone. When this is done, only 1283/3221 targets are threadable; this reflects the fact that often the template with the best match to the native
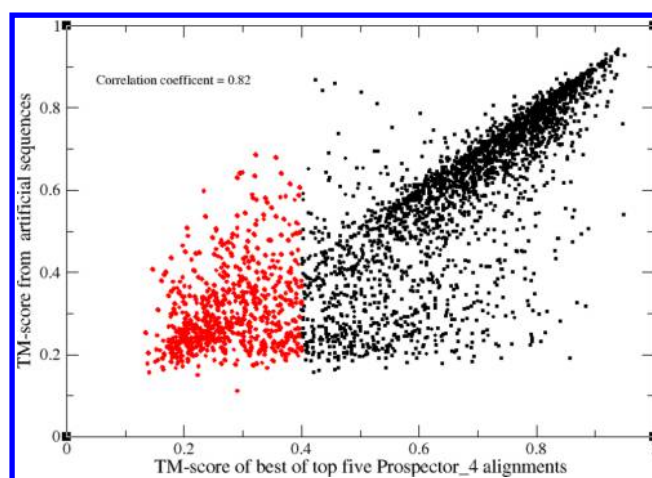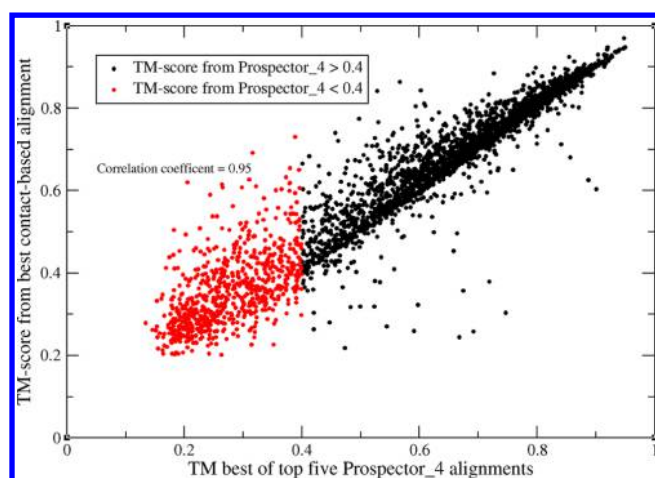


**Figure 5.** TM-score of the best of the top 5 ranked PROSPECTOR_4 threading template alignments obtained for artificial target and template protein sequences versus that when native protein sequences are used. Black (red) circles indicate (non) threadable proteins using native target and template sequences as input.

protein's secondary structure does not have the same global fold as the target. When we use secondary structure plus pair potential terms to drive the threading alignment, then 2066/3221 targets are threadable. This suggests, not surprisingly, that the selection of sequences is strongly influenced by tertiary interactions, a rather reasonable result. However, for this method to work, pairwise residue contacts have to be preserved at an appropriate level between the target and template structures. On the basis of this conjecture, we now examine what happens when contact map alignment is done and whether this will provide deeper insight into what constitutes a threadable versus a nonthreadable protein target.

**Analysis of Threadability in Contact Map Driven Alignments.** In what follows, we employ the native contacts of the target sequence to generate the best contact map alignment to the template. This is being done deliberately, as we are seeking to understand why certain protein structures are threadable, whereas others are not. If one cannot generate native like alignments even when all the contacts are native, then the performance when predicted contacts are used (which is the actual situation) will certainly be worse. Consider the cases of the top 5 templates selected from threading versus the best structural alignments. For threading selected templates, C-align generates predictions whose best of the top 5 ranked alignments has a TM-score ≥0.4 for 2614 targets versus 2949 targets when the best nontrivial (sequence identity <0.3) structural alignment, SA, template identified from fr-TM-align is used. Figure 6 shows the correlation between the C-align generated best TM-score and the PROSPECTOR_4 best TM-score for the same set of threading templates. Clearly, the two sets are highly correlated with a correlation coefficient of 0.92. Once again, independent of the particular method used to generate the alignment, the quality of the results depends on the particular target structure chosen. The question then is what makes a given structure threadable or not. We next turn to the analysis of this key question.

Let us first examine the performance of C-align using the top 5 templates selected not from threading but from the best structural alignment. Despite the fact that fr-TM-align generates structures whose TM-score ≥0.4 in every case, C-align still yields 247 nonthreadable targets. In contrast, if the

**Figure 6.** TM-score of the best of the top 5 ranked PROSPECTOR_4 threading template alignments obtained from contact map based alignment vs that when threading is used. Black (red) circles indicate (non-) threadable proteins using native target and template sequences as input.

PROSPECTOR_4 selected templates are used, then there are a total of 581 nonthreadable targets despite the fact that the target structure's native contacts are used to drive the alignment. In Figure 7, we present the distribution of the
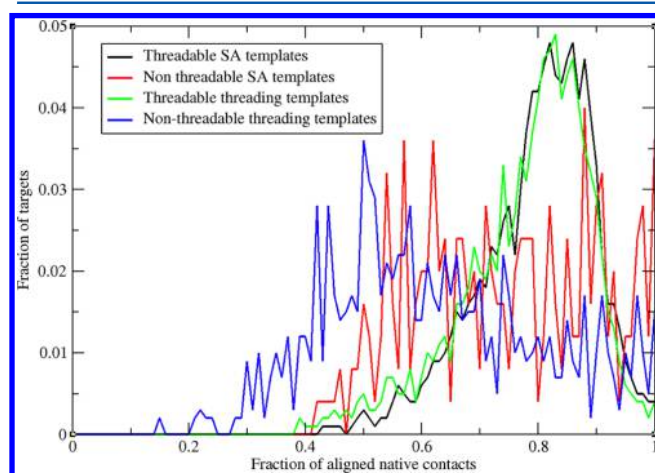


**Figure 7.** Distribution of the fraction of targets versus the fraction of aligned native contacts generated by C-align for the best of the top 5 templates identified using the fr-TM-align structural alignment algorithm and by PROSPECTOR_4.

fraction of aligned native contacts obtained in each case. For templates obtained from the best structural alignments, the p-value of Student's $t$ test for threadable and nonthreadable proteins is 0.96. This is the same p-value obtained for that between threadable and nonthreadable PROSPECTOR_4 generated templates. Thus, the difference in the distributions of the fraction of aligned native contacts for each of the two respective distributions is not statistically significant. Put another way, for evolutionarily distant proteins, due to structural differences, the aligned native contact fractions behave similarly. For threadable proteins, these templates bear a significant global structural similarity to native, whereas for nonthreadable ones they do not. When structural alignment selected templates are used, for the 247 nonthreadable targets, there is an alternative high scoring alignment generated such

that the resulting aligned coordinates have a TM-score <0.4 to the native fold (see black vs red curves). One can even have very high contact map overlap (see fc >0.9). There are nonthreadable targets where all native contacts are aligned; e.g., 1bbt4 whose TM-score = 0.22. These proteins tend to be small and have very open, nonglobular protein conformations. In fact, 26% (65/247) of these nonthreadable proteins are ≤60 residues in length. In contrast, for templates identified on the basis of their structural alignment to native, about 8% of threadable proteins are in this size range. Clearly, smaller proteins contain a smaller number of contacts and secondary structure elements that can be aligned, and the possibility of finding a globally dissimilar structure that satisfies these constraints is large. These small proteins need to be accounted for in any threading alignment algorithm. For threading identified templates, the fraction of threadable proteins ≤60 residues in length drops to 6% of the total number of threadable proteins, and the number of such small, non-threadable targets essentially doubles to 131/581, with a somewhat reduced fraction of 23%. Of course, this is just part of the story, but the qualitative effect remains unchanged.

While it is certainly true on the basis of Figure 7 that on average there are more templates whose $f_N$ exceeds 0.6 (95%) in threadable than in nonthreadable template (88%) structural alignment, SA, identified templates; nevertheless, there is considerable overlap. Similarly, for PROSPECTOR_4 identified templates, we can confidently assign a protein as being nonthreadable when $f_N < 0.6$ (<93% of threadable targets exceed this value, whereas 49% of nonthreadable targets do). However, since the two $f_N$ distributions overlap significantly, contact overlap criteria cannot be reliably used to differentiate threadable from nonthreadable proteins. In nonthreadable cases, at a given $f_N$ even when the same template as that giving the best structural alignment is used, a poor alignment will result. Other folds, that tend to be larger, suffer from less $f_N$ redundancy, and as such are more likely to be threadable. Thus, whether or not a protein is threadable simply depends on whether its fold is such that high $f_N$ scoring templates adopt the native fold or not. For nonthreadable proteins, given differences in the structure of the target and the template, there are non-native folds with very similar $f_N$ values, whereas, for threadable proteins, the best scoring folds have a similar structure to the target.

## ■ DISCUSSION AND CONCLUSION

The qualitatively similar performance of different threading algorithms on the same set of threading targets strongly suggests that there are common features of the proteins that are threadable (those having good quality alignment to native, taken here as a TM-score ≥0.4) when there are no closely related proteins in the template library. This issue is relevant in that threading based structure prediction methods seem to have hit a plateau, and it is important to understand why this is the case. Does it reflect a fundamental limitation of the approach, or is it just a matter of the structural completeness of the template library? Of course, as the number of protein structures and sequences continues to grow, eventually, there will be no distantly related threading templates, and one would expect threading to work in general. In the interim, however, when a significant fraction of an arbitrary exome has over half of its sequences in the distant homology regime to the PDB, this is a critical issue if structure prediction is to be able to assist in the annotation of protein function.[35]

Thus, there is a clear need to identify why contemporary threading methods fail on the certain targets. Here, we showed that, even for nonthreadable proteins, there are structurally related template proteins in the PDB. We also eliminated that trivial explanation that nonthreadable targets are more evolutionarily distant from their templates than threadable ones by showing that the behavior of artificially generated sequences selected for their stability in the structure of interest are highly correlated with that of native proteins. Since these artificial sequences are not related to each other by evolution and have the same sequence diversity, this suggests that it is mainly the properties of the protein's structure that make it threadable or not. Furthermore, even when a pair of proteins are matched by threading, one cannot conclude that they are evolutionarily related, as the artificial proteins are clearly unrelated by evolution yet they match as well.

Motivated by the results from the artificial sequences, we sought a structure based solution to the question of threadability. Clearly, aligning secondary structure is not informative, as there are many different folds with essentially the same secondary structure pattern and length of secondary structure elements. We then focused on contact map alignment and found that the results in most consonance with direct target-template structure alignments involve the use of contact maps between $C\alpha$ atoms defined at the 8.5 and 14 Å cutoff level. This generates alignments whose TM-scores are highly correlated with those obtained from threading. What is clear is that the distribution of the fraction of aligned native contacts is very similar in both threadable and nonthreadable templates. Put succinctly, there are very high scoring alignments in nonthreadable templates that result from differences in the target and template structures. When the native structure is used, almost all targets have a contact alignment based TM-score $\geq 0.95$. When structural alignment selected templates whose sequence identity to the target protein <30% are used, then, for the majority of cases, good alignments are generated, but for 7.6%, poor quality alignments are generated. However, in many cases, these have a high fraction of native contacts. A significant number of these nonthreadable folds are small proteins of low fold complexity, but this is not always so. Rather, nonthreadable proteins simply reflect the fact that the average fraction of these native $C\alpha$ contacts does not uniquely specify the native state. That is, it is a too coarse grained measure. While in the majority of cases it is the native fold which is recovered, in a minority (15%), there is an alternative alignment which has a higher contact fraction that that of the native alignment and threading fails. Despite our attempts to tease out a single cause as to why some folds are nonthreadable, we were unable to find it. Rather, nonthreadable protein structures often have a synergistic combination of effects: small proteins with a small number of secondary structural elements, low fold complexity, low contact order, and sometimes just the fact that a non-native fold has better contact map overlap than native like folds.

What then are possible avenues of improvement when secondary structure and native contact overlap are insufficient to select the native fold? This reflects the implicit assumption of any threading approach that, when an appropriate comparison metric is high, the more likely it is that native like features are recovered. It is an open question whether side chain contacts can be routinely predicted by residue covariation[40,41] with sufficient accuracy for enough targets that the coverage of nonthreadable targets can be improved. However, perhaps

similar problems as those encountered by threading will be observed. As demonstrated here, even when all nonlocal contacts are satisfied, alternative non-native alignments can be generated for certain structures. More generally, we could turn the question around. Rather than asking what is the property of nonthreadable target structures, we could ask (in the twilight zone of sequence identity) if there are certain templates that when matched by threading are almost always indicative that the target protein is nonthreadable. This can provide another means of assessing the reliability of threading in advance and possible sets of alternative folds consistent with the identified, nonthreadable template. For targets mapped to these non-threadable templates, template free methods will need to be applied, as threading based approaches are not reliable. In this way, the manifold of nonthreadable templates could be exploited to provide additional information. Alternatively, perhaps methods that could predict higher order patterns of contacts or global contact maps might sometimes be of help in the regime where there is roughly 50−60% overlap and yet the folds differ. What is clear, however, is that traditional approaches to threading have more or less realized their maximum potential, and different methods need to be developed to deal with the 15−20% of targets that remain outside the reliable regime of current structure prediction methods. This remains a crucial problem that needs to be addressed.

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### Author Contributions
The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript. J.S. conceived of the idea and performed the majority of the calculations and analysis. H.Z. performed the threading calculations using the HHpred and SP$^3$ threading algorithms.

### Notes
The authors declare no competing financial interest.

## ■ ACKNOWLEDGMENTS

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