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## Topological defects govern crack front motion and facet formation on broken surfaces

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## Supplementary figures and movies

Supplementary Figure 1. The parameters W and  $\alpha$  extracted from isolated step-lines. (a) Values of W are concentrated around  $W = 50^{+10}_{-3}\mu m$ . (inset) W is determined by measuring the distance between the minimum and the maximum of the front derivative  $\partial x/\partial z$ . (b)  $\alpha$  (asymmetry) values determined from front profiles by fitting to  $\delta x(z) = cz + \frac{H}{\pi} \left[ \frac{1}{2} log \left( 1 + \frac{4z^2}{W^2} \right) \pm \alpha \arctan\left( \frac{2z}{W} \right) \right]$  assuming a constant  $W = 50\mu m$ . The distribution yields  $\alpha = 0.24 \pm 0.08$ 



Supplementary Figure 2. Step width w grows with step height h. Blue bars show the range of w measured by profilometry when averaged over  $2\mu m$  intervals of h. Linear regression (red line) yields a proportionality coefficient of  $1.4 \pm 0.4$ . The dashed black line, w = h, is one standard deviation below the mean. (*inset*) Number of data points within each  $2\mu m$  interval of h. A total of ~155,000 points was considered.





*Supplementary Figure 3.* **Dependence of step-line direction on the normal to the crack front.** (a) A typical fracture surface in the faceting regime. (b) A section of a fracture surface in (a) with a step-line extending nearly parallel to the X axis highlighted in yellow. Numbers refer to curved points along the front in (c). The dotted light blue line approximates the front tilt in (c). (c) A snapshot of the crack front that created the surface in (b) reveal strong tilting of the front.



Supplementary Figure 4. (a) The height profile along the z axis of a fracture surface containing a single step (at  $z \sim 2500 \mu m$ ) taken at a constant x. Except at the step, surface height barely changes, and the wavelength of its variation is of the order of the sample thickness (~ 4.6 mm). (b) The same height profile with the y axis blown-up by a factor of 45.

Supplementary Movie 1. Propagation of a crack front forming a single step-line at steady state over 50ms (interval between frames is 0.5ms) (see Fig. 2(a,d)).

*Supplementary Movie 2.* Propagation of a crack front throughout the simultaneous nucleation and growth of two step lines over 30*ms* (interval between frames is 0.3*ms*) (see Fig. 2(b,e)).

Supplementary Movie 2. Propagation of a crack front during the merging of two step-lines over 25ms (interval between frames is 0.3ms) (see Fig. 2(c,f)).